



Pattern  
Recognition  
Lab



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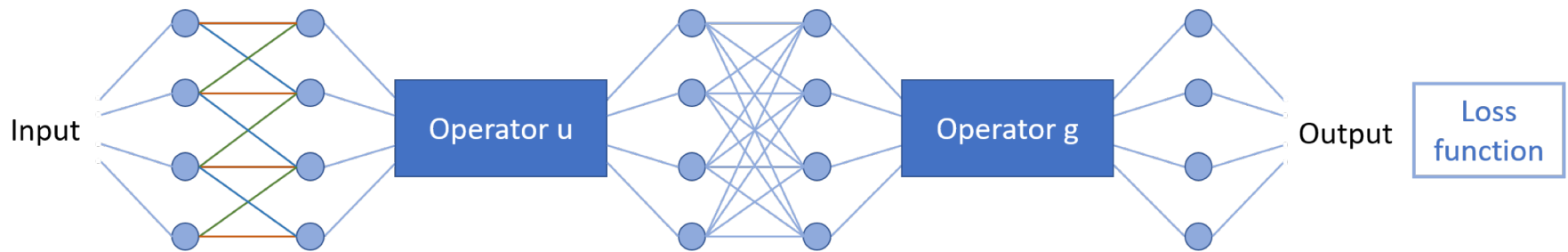
# Python Reconstruction Operators in Neural Networks

PYRO-NN



# Motivation

- Use of known operators !

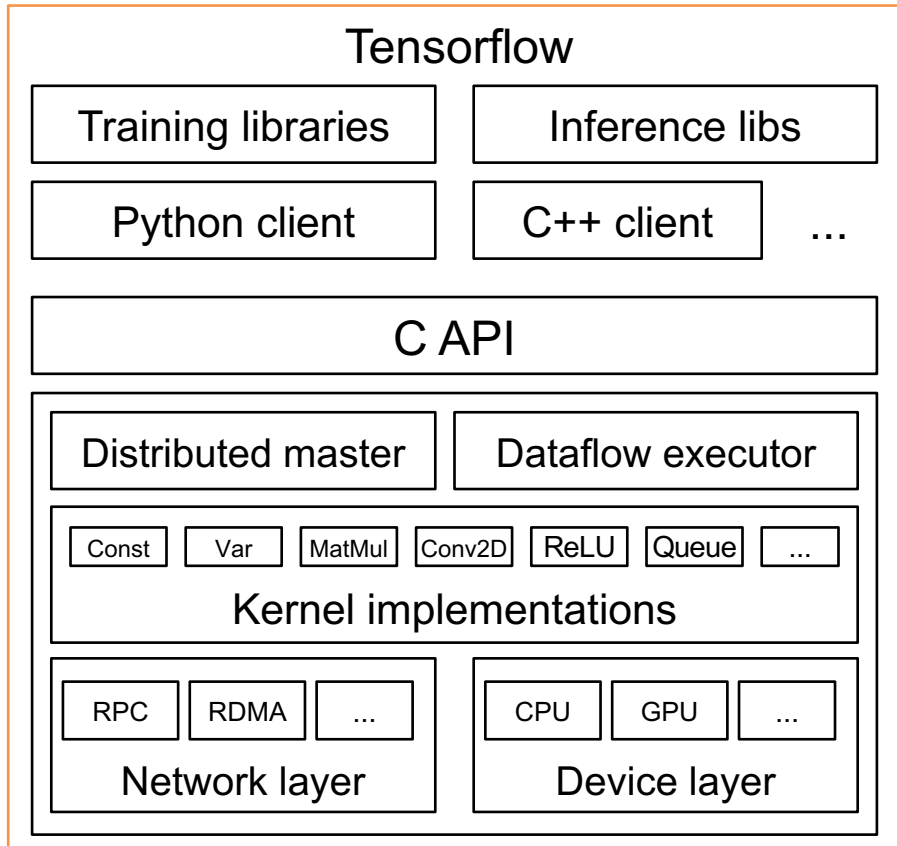


- Reduce error, amount of paramter
- Gain interpretability
- Gradient flow through different domains

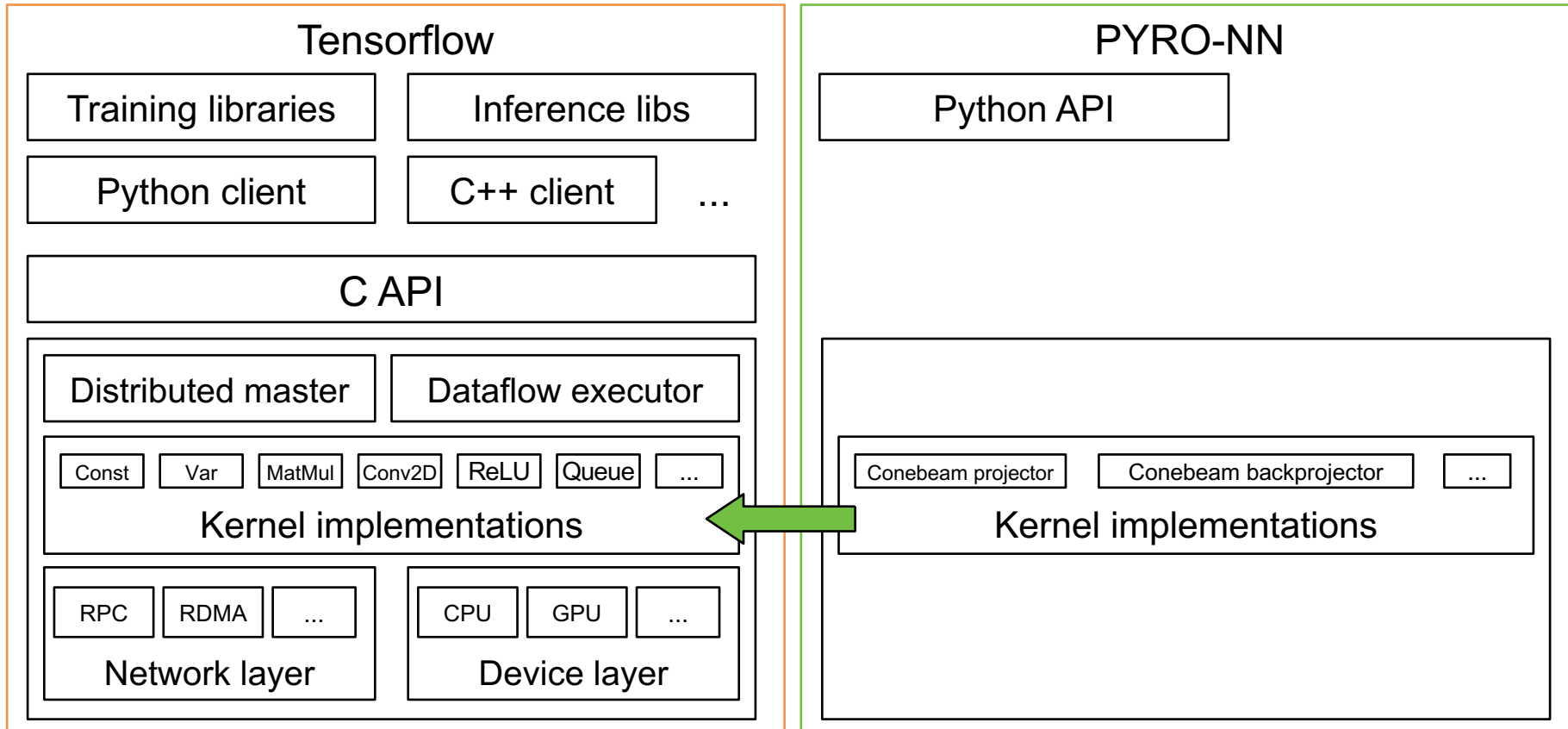
# PYRO-NN: Python Reconstruction Operators in Neural Networks

- TF-Layers: Projector and back-projectors
  - 2D parallel, fan and 3D cone-beam
- Python API:
  - Layer abstraction
  - Geometries
  - Phantoms
  - Data generators

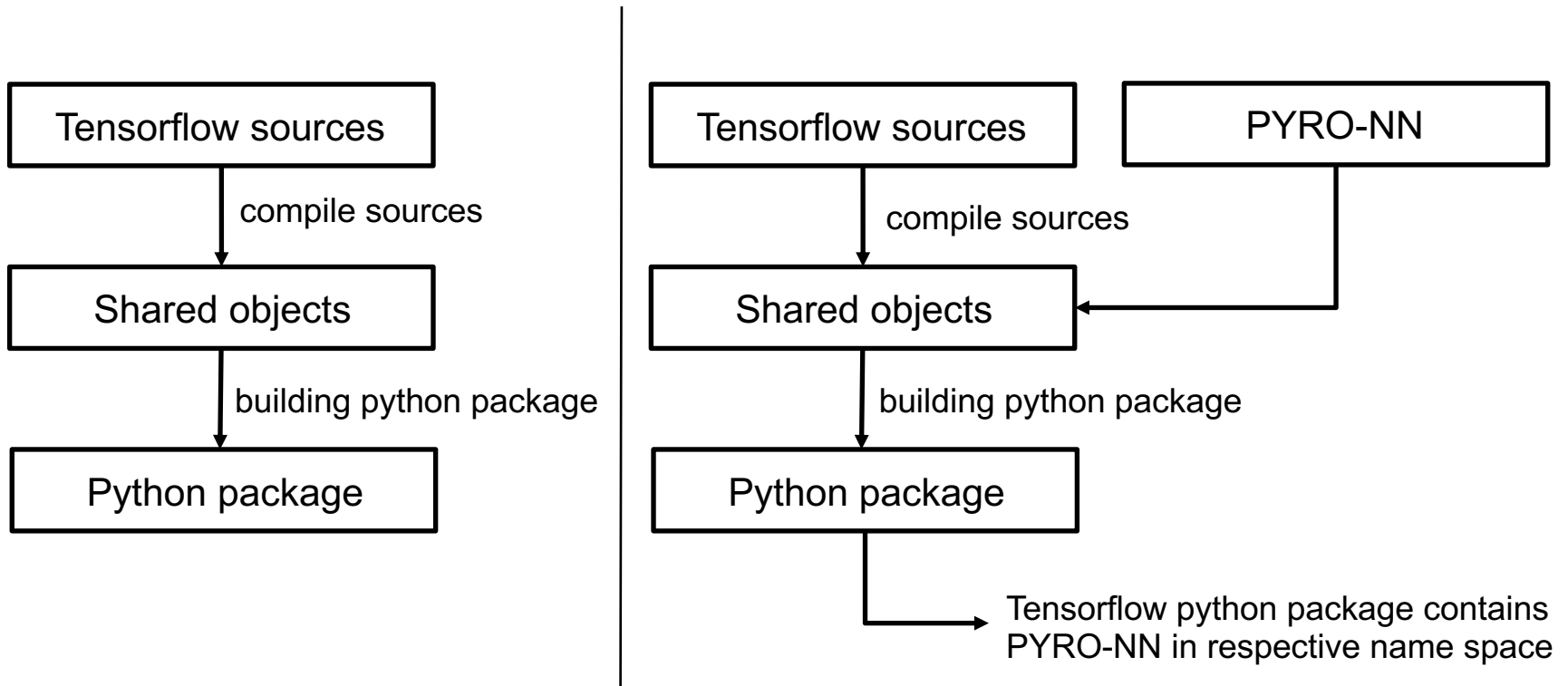
# Operators in Tensorflow



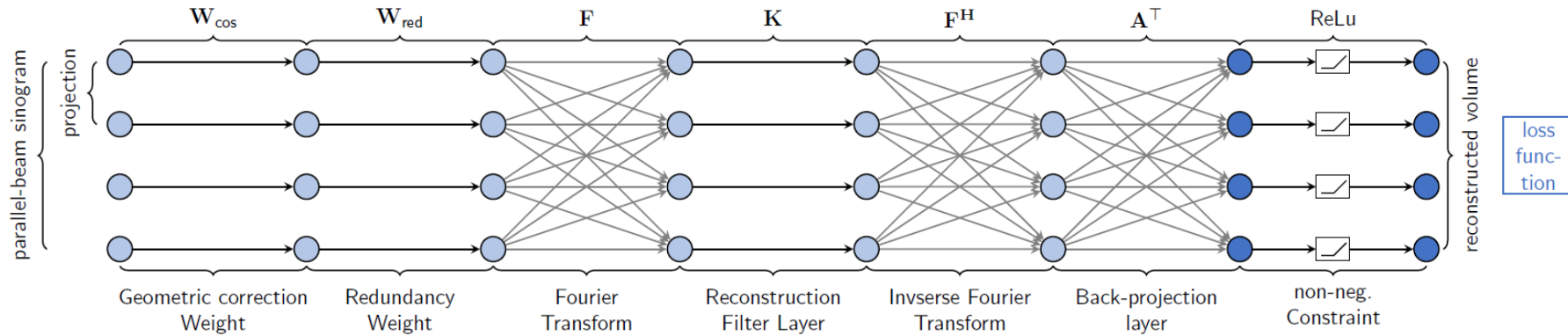
# Known Operators in Tensorflow



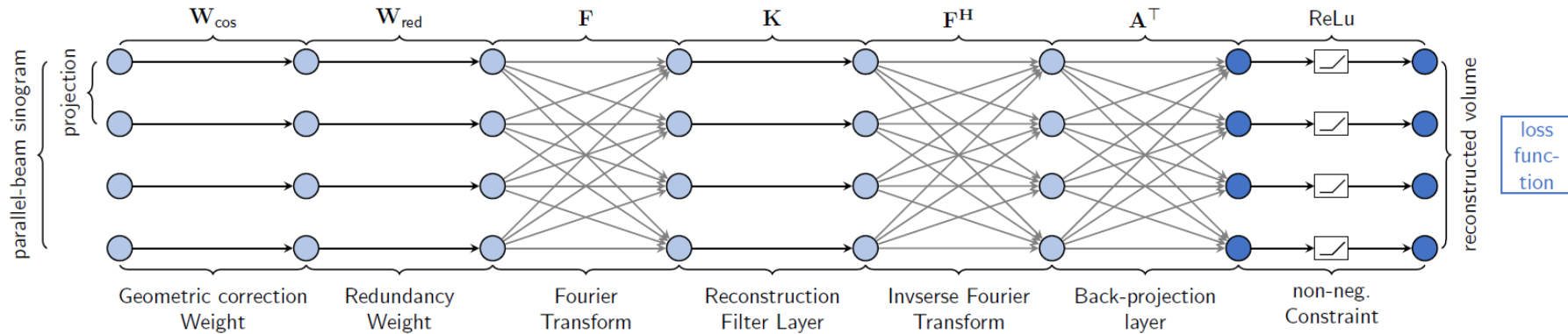
# PYRO-NN Architecture



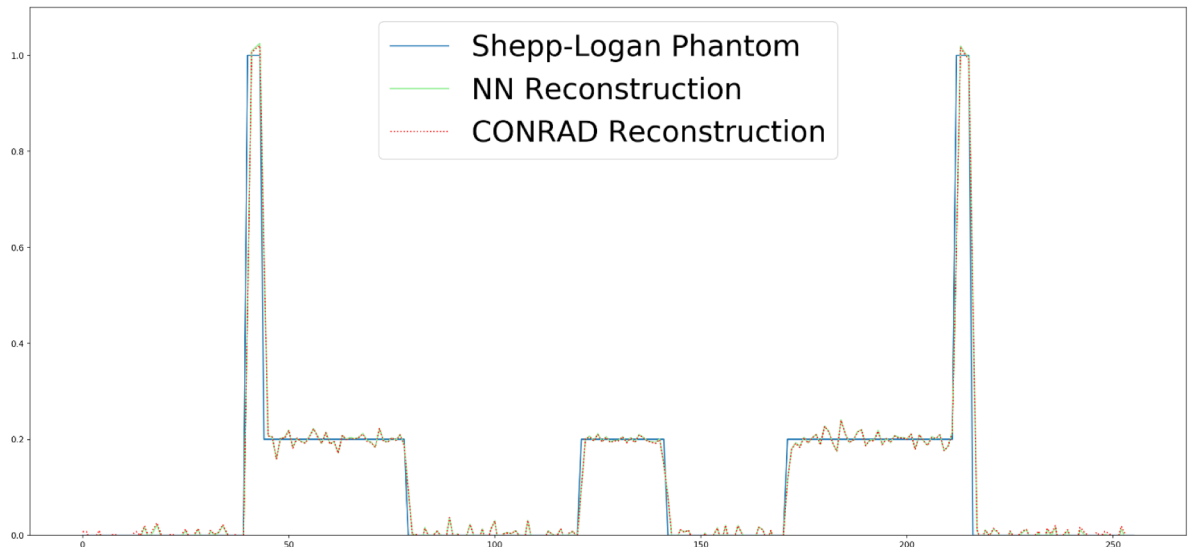
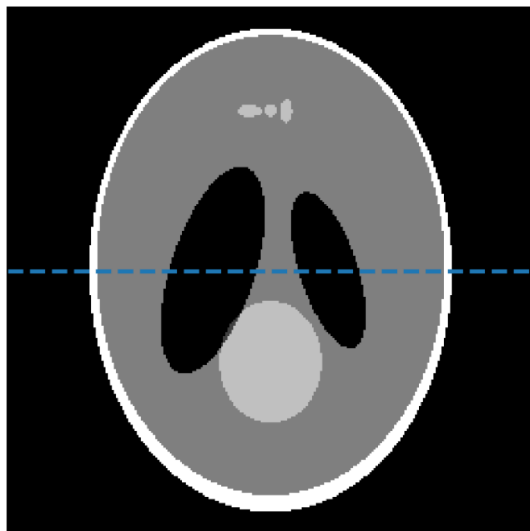
# Short-Scan FDK-Net



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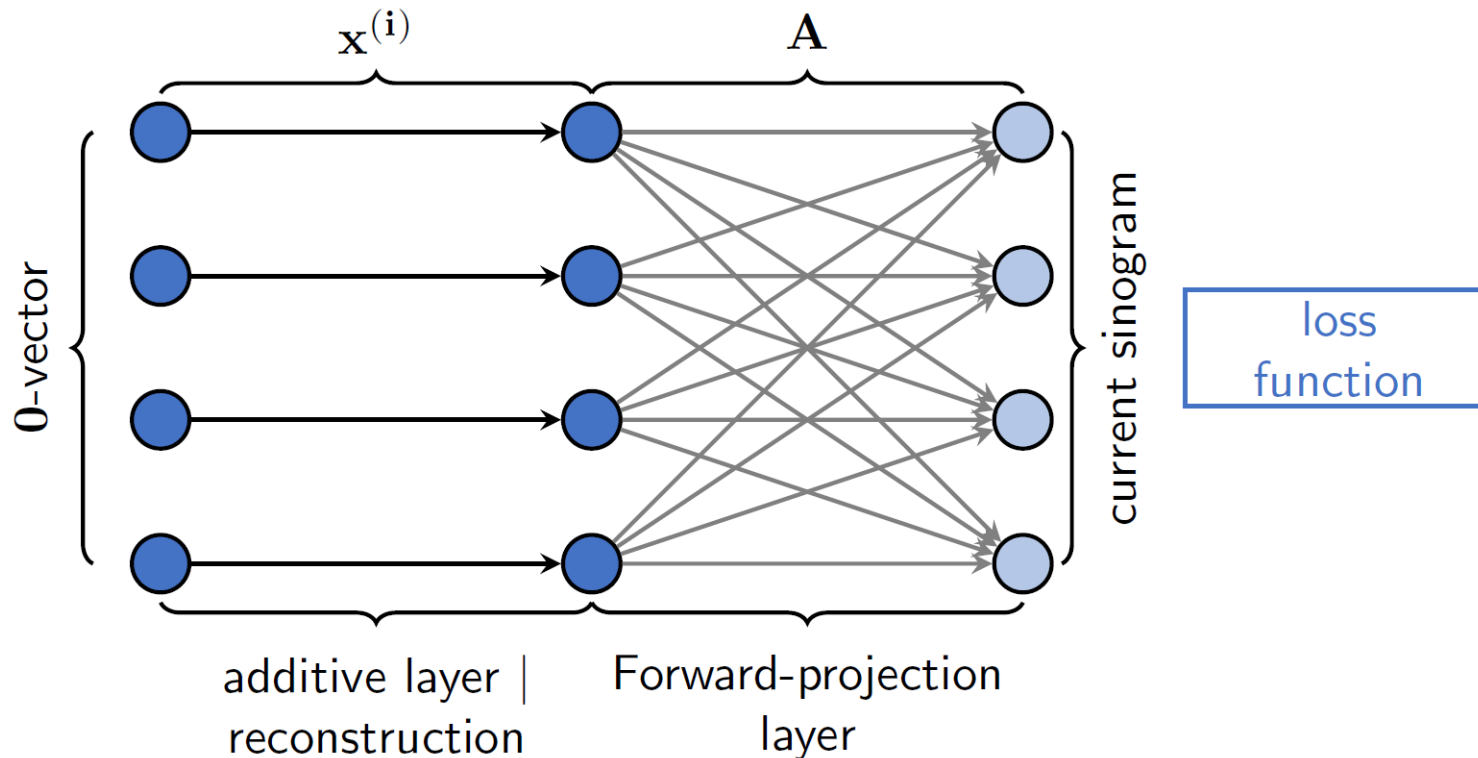
Central Slice NN Reconstruction





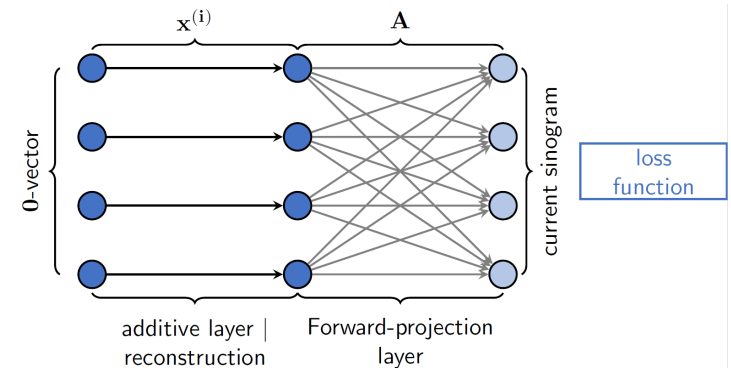
# Iterative Reconstruction

$$\min \|Ax - p\|_2^2 + \lambda \text{TV}(x)$$



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$$\min \|Ax - p\|_2^2 + \lambda \text{TV}(x)$$

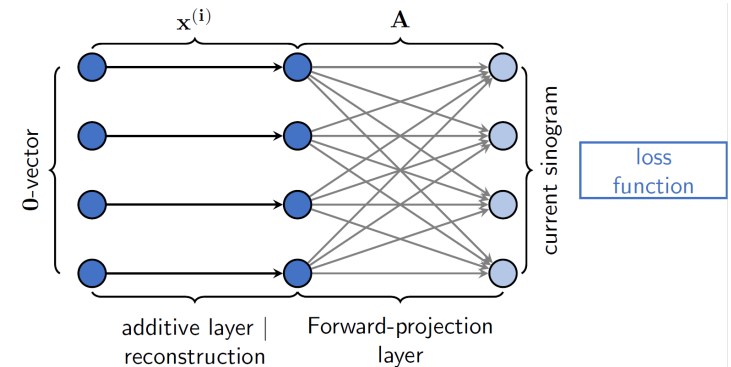


```
from pyronn.ct_reconstruction.layers import projection_2d
```

```
reco = tf.get_variable(
    initializer=np.zeros(geometry.volume_shape),
    trainable=True,
    constraint=lambda x: tf.clip_by_value(x, 0, np.infty))
```

# Iterative Reconstruction

$$\min \|Ax - p\|_2^2 + \lambda \text{TV}(x)$$



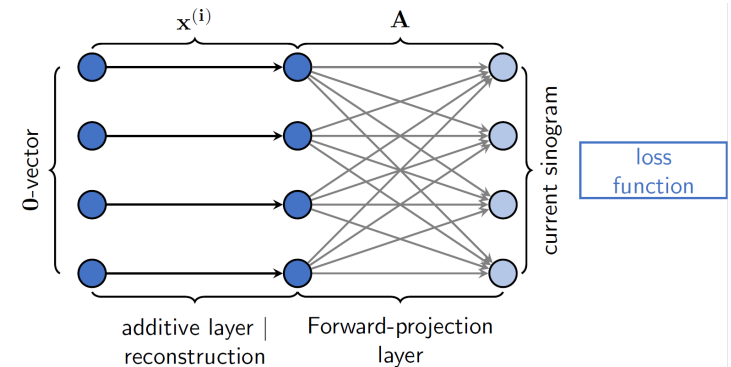
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current_sino = projection_2d.parallel_projection2d(reco, geometry)
```

# Iterative Reconstruction

$$\min \|Ax - p\|_2^2 + \lambda \text{TV}(x)$$



```

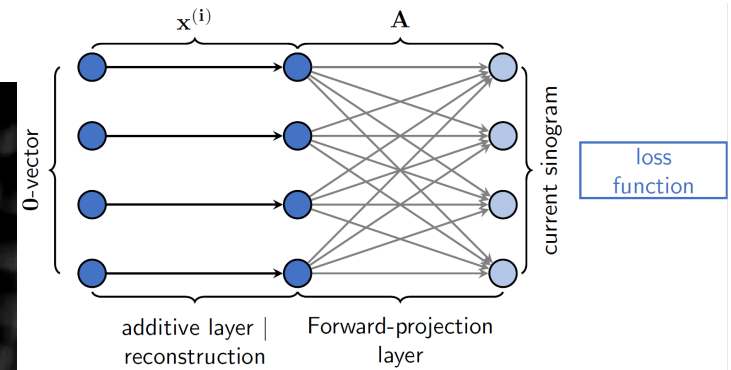
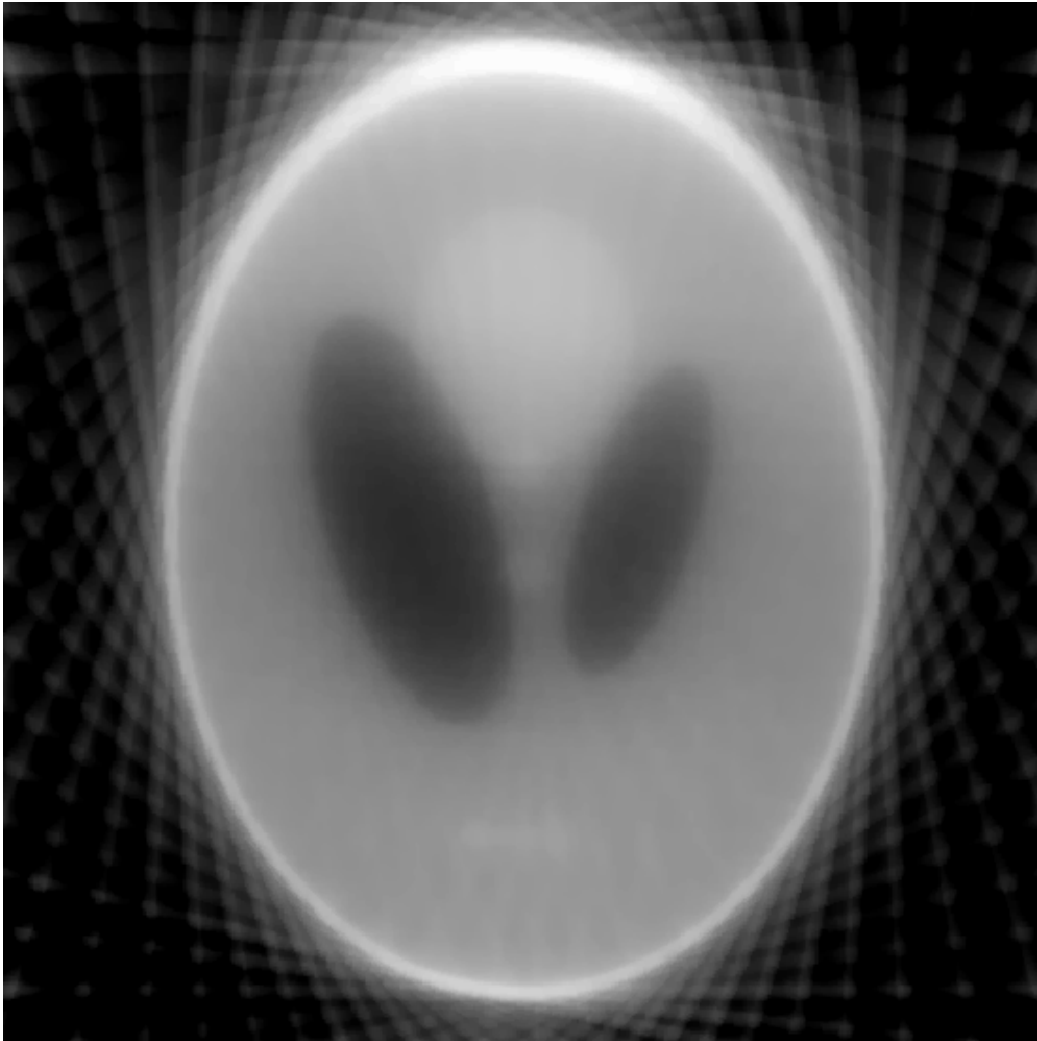
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current_sino = projection_2d.parallel_projection2d(reco, geometry)

error = tf.squared_difference(current_sino, acquired_data)
        + lambda * tf.image.total_variation(reco)
    
```

# Sparse View CT



# PYRO-NN on GitHub

Python API:

<https://github.com/csyben/PYRO-NN>

Layers:

<https://github.com/csyben/PYRO-NN-LAYERS>



# PYRO-NN

## PYTHON RECONSTRUCTION OPERATORS FOR NEURAL NETWORKS

- Supports Tensorflow and PyTorch
- Full GPU Integration
- Open Source
- Apache 2.0 License

pip install pyronn

### FBP Reconstruction

```

def model(self, sinogram):
    self.sinogram_cos = tf.multiply(sinogram, self.cosine_weight)
    self.redundancy_weighted_sino = tf.multiply(self.sinogram_cos, self.redundancy_weight)

    self.weighted_sino_fft = tf.fft(tf.cast(self.redundancy_weighted_sino, dtype=tf.complex64))
    self.filtered_sinogram_fft = tf.multiply(self.weighted_sino_fft, tf.cast(self.filter, dtype=tf.complex64))
    self.filtered_sinogram = tf.real(tf.ifft(self.filtered_sinogram_fft))

    self.reconstruction = cone_backprojection3d(self.filtered_sinogram, self.geometry, hardware_interp=True)

    return self.reconstruction, self.redundancy_weighted_sino
    
```

### TV Recon

```

def model(self, input_volume):
    self.updated_reco = tf.add(input_volume, self.reco)
    self.current_sino = projection_2d.parallel_projection2d(self.updated_reco, self.geometry)
    return self.current_sino, self.reco

tv_loss_x = tf.image.total_variation(tf.transpose(self.current_reco))
tv_loss_y = tf.image.total_variation(self.current_reco)

self.loss = tf.reduce_sum(tf.squared_difference(self.label_element, self.current_sino)) + self.regularizer_weight*(tv_loss_x+tv_loss_y)
    
```